Book Chapter

Computational Experiments on the Step and Frequency Responses of a Three-Axis Thermal Accelerometer

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Abstract

The sensor response has been reported to become highly nonlinear when the acceleration added to a thermal accelerator is very large, so the same response can be observed for two accelerations with different magnitudes and opposite signs. Some papers have reported the frequency response for the horizontal acceleration to be a first-order system, while others have reported it to be a second-order system. The response for the vertical acceleration has not been studied. In this study, computational experiments were performed to examine the step and frequency responses of a three-axis thermal accelerometer. The results showed that monitoring the temperatures at two positions and making use of cross-axis sensitivity allow a unique acceleration to be determined even when the range of the vertical acceleration is very large (e.g., $-10,000$ – $10,000$ g). The frequency response was proven to be a second-order system for horizontal acceleration and a third-order system for vertical acceleration.

Keywords

Thermal Accelerometer; Computational Fluid Dynamics; Cross-Axis Sensitivity; Step Response; Frequency Response; Nonlinearity

Introduction

Thermal accelerometers have recently attracted much attention and become the subject of theoretical, numerical, and experimental studies. Because thermal accelerometers do not have a proof mass, they can endure a higher shock than accelerometers that do have a proof mass. With a proof mass, a squeeze film effect is caused between it and the accelerometer structure, which requires a complex package to be removed.

A thermal accelerometer is based on the displacement of a hot air bubble generated by a heated wire in an enclosed chamber under acceleration. The principle of detecting x - y (i.e., horizontal) accelerations has been explained by others [1–4]. In short, two temperature sensors are positioned in parallel on a horizontal plane, and a heater is placed between them (Figure 1a). When no acceleration is applied to the accelerometer, the heater creates a symmetric heat bubble so that the same temperature is obtained by the two temperature sensors (Figure 1b). However, when a non-zero value of acceleration a_x in the x -direction is applied to the accelerometer, the shape of the heat bubble is distorted by the buoyancy effect. Consequently, the temperature difference ΔT_x is detected (Figure 1b). By knowing the relation between a_x and ΔT_x in advance, the arbitrary value of the acceleration added to the accelerometer can be calculated from the measured temperature difference ΔT_x . The acceleration in the y -direction can be measured in a similar manner.

Figure 1: Principle to detect x - y (horizontal) accelerations: (a) heater and temperature sensors; (b) temperature profiles with and without acceleration.

To measure the acceleration in the z -direction (i.e., vertical direction), a few methods are available in the literature. A straightforward and simple method is to place the heater and temperature sensors on a vertical or inclined plane [5]. The second method is shown in Figure 2a; the heater and two temperature sensors are placed on three layers the same distance apart [6]. When neither acceleration nor gravity is applied to the accelerometer, a spherical heat bubble is created (i.e., the gray-filled circle), and the two sensors show the same temperature. As an example, however, if an acceleration of $+1\text{ g}$ in the positive z -direction is applied, the heat bubble moves in the positive z -direction owing to the buoyancy effect (i.e., ellipse with solid line). Thus, the two sensors detect different temperature values, and the acceleration is determined by the temperature difference. The disadvantage of this method is that it takes up more space than the next method described below.

Figure 2b shows the third method. A cavity structure is created that is asymmetric in the up and down directions [7–10], and heat and temperature sensors are placed on the same plane. Because the shape of the deformed heat bubble varies according to the magnitude and sign of the acceleration in the z -direction, the measured temperature can determine the magnitude and sign of the acceleration. When the acceleration is very large, however, Nguyen et al. [10] pointed out that “the sensor response is highly non-linear,” such that “the same response can be observed for two accelerations with different magnitudes and

opposite signs.” Therefore, it is impossible to determine which acceleration is correct when this response is observed with an accelerometer. The first purpose of this study was to address this difficulty by making use of cross-axis sensitivity, which we demonstrated in a computational experiment.

Figure 2: Principle to detect z (vertical) accelerations: (a) symmetric and (b) asymmetric structures.

Courteaud et al. [3] treated the frequency response of the accelerometer for the horizontal acceleration as a first-order system. On the other hand, Silva et al. fitted this frequency response to the curve of a second-order system (Figure 4 in [11]). Garraud et al. [4] and Nguyen et al. [10] studied the frequency response of the accelerometer but did not refer to the order of the system. Furthermore, none of the above studies considered the response for vertical acceleration. The second purpose of this study was to demonstrate, through a computational experiment, that the frequency response is a second-order system for horizontal acceleration and a third-order system for vertical acceleration. However, in this study, we did not try to improve the sensitivity of our thermal accelerometer, and we did not examine the effect of nonlinearity on the sensitivity.

Steady-State Step Response

Computational Model of the Accelerometer

Figure 3a shows the 3D view of our model for the computational experiment, and Figure 3b–d respectively show the side, top, and isometric views of the simplified schematic. The cavity structure was asymmetric in the up and down directions as in [7–10]. The

heater loop consisted of four circular arcs subtending 45° and placed on a circle with a radius of $0.4 L$, where L is the reference length. The temperature sensors X1 and X2 for detecting acceleration in the x -direction and Y1 and Y2 for detecting acceleration in the y -direction were located outside the heater loop and, importantly, at a small elevation from the heater plane to obtain a better signal [7]. The sensors for the z -direction were located inside the heater loop. The positions of these sensors were found to be optimal based on a computational experiment that was performed in advance [7]. The device was packaged in a sealed chamber containing the working medium, in this case air (although helium can be used as well).

Figure 3: Computational model of the accelerometer: (a) 3D view; (b–d) side, top, and isometric views.

Equations and Computational Method

To capture the density–temperature dependence due to a large temperature change, the conservation laws of mass, momentum, and energy for a compressible fluid were employed to describe the thermofluidic phenomena in the accelerometer. These can be expressed as follows:

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{u}) = 0 \quad (1)$$

$$\frac{\partial (\rho \mathbf{u})}{\partial t} + \mathbf{u} \cdot \nabla \cdot (\rho \mathbf{u}) = -\nabla p + \nabla \cdot (\mu \nabla \mathbf{u}) \quad (2)$$

and

$$\frac{\partial (\rho c_p T)}{\partial t} + \mathbf{u} \cdot \nabla \cdot (\rho c_p T) = \nabla \cdot (\lambda \nabla T) \quad (3)$$

where u , p , and T are the velocity vector, pressure, and temperature, respectively, of the fluid flow, and ρ , c_p , μ , and λ are the density, specific heat, viscosity, and thermal conductivity, respectively, of the fluid. To close the equations, we assumed that the working fluid obeys the ideal gas law for compressible flows:

$$p = \frac{\rho R T}{M} \quad (4)$$

where R is the universal gas constant, and M is the molar mass of the gas.

The computation region of the accelerometer was decomposed into a hexagonal mesh, as shown in Figure 4, with the mesh generation software ANSYS ICEM CFD. The mesh number was 674,015, which is large enough to obtain accurate solutions [7]. Flow parameters such as u , p , and T for this mesh were then obtained with the computational fluid dynamics package ANSYS Fluent, and the finite volume method was used to discretize the governing Equations (1)–(4). The SIMPLeC method was adopted for pressure–velocity coupling, and all spatial discretizations were performed with the second-order center scheme. The heaters were simulated as a solid zone with a constant heat generation rate.

Figure 4: Computational mesh: (a) side and (b) top views.

Conditions and Results

For the computational experiment, the length L (Figure 3) was set to 1 mm, and the temperatures on the wall and heater were respectively kept at 300 K and 500 K. The working medium was air. The accelerations in the x -direction a_x , and y -direction a_y that were added to the accelerometer were 0 g, +1 g, +2 g, +3 g, +4 g, +5 g, +10 g, +20 g, +50 g, +100 g, and +200 g. Only positive values were adopted because the temperature measured at temperature sensor X2 (Figure 3) for positive acceleration in the x -direction was the same as that measured at temperature

sensor X1 for negative acceleration in the x-direction owing to the symmetric structure in both the x- and y-directions. Thus, the response to the negative accelerations could be obtained by the response to the positive accelerations. On the other hand, the accelerations in the z-direction a_z were set to both positive and negative values: 0 g, ± 1 g, ± 2 g, ± 3 g, ± 4 g, ± 5 g, ± 10 g, ± 20 g, ± 50 g, ± 100 g, and ± 200 g. This was because of the asymmetric structure in the z-direction. For all computational experiments, these constant accelerations were suddenly added at time 0 to the accelerometer under no acceleration (time < 0). Only the steady state of the step response was considered.

Figure 5 shows two examples of temperature contours on the x - z plane when (a) no acceleration or gravity was added to the accelerometer and (b) an acceleration of 200 g was added only in the x -direction. The heat bubble that was symmetric under no acceleration showed remarkable deformation with a large acceleration due to the buoyancy effect. We defined ΔT_{X1} and ΔT_{Z1} as the differences between temperatures measured by temperature sensors X1 and Z1, respectively, with gravity only and with the added acceleration.

Figure 5: Temperature contours on the x - z plane: (a) $(a_x, a_y, a_z) = (0g, 0g, 0g)$; (b) $(a_x, a_y, a_z) = (200g, 0g, 0g)$.

Figure 6 shows the relation between the temperature difference ΔT_{x1} and x -acceleration a_x , with the y -acceleration $a_y = 0g$, and with three z -accelerations $a_z = 0g, 200g$, and $-200g$. The absolute value of ΔT_{x1} increased but not linearly with the absolute value of the x -acceleration a_x . The three curves were not on one curve because of the cross-axis sensitivity of the z -acceleration affecting ΔT_{x1} . As shown below, this sensitivity is not a problem when obtaining the acceleration from the temperature difference.

Figure 6: Relations between ΔT_{x1} and x -acceleration a_x , with y -acceleration $a_y = 0g$, and with z -accelerations $a_z = 0g, 200g$, and $-200g$.

Figures 7 and 8 show three-dimensional plots of ΔT_{x1} and ΔT_{z1} produced by the accelerations combined with a_x (from 0 g to 200 g) and a_z (from -200 g to 200 g). The y -acceleration was kept at $a_y = 0$ g. The black dots on the curved surfaces represent the data obtained by the computational experiments. These surfaces were not flat, so the relation between the outputs ΔT_{x1} and ΔT_{z1} and the inputs a_x and a_z were not linear. Cross-axis sensitivity was also observed. The temperature difference in the x -direction ΔT_{x1} obtained by the sensor for the x -acceleration was affected by the z -acceleration, and ΔT_{z1} was affected by the x -acceleration. However, cross-axis sensitivity and nonlinearity are not a problem when calculating the acceleration from the measured temperature, as explained below.

Figure 7: Three-dimensional plot of ΔT_{x1} created by the accelerations of a_x (from 0 g to 200 g) and a_z (from -200 g to 200 g).

Figure 8: Three-dimensional plot of ΔT_{z1} created by the accelerations of a_x (from 0 g to 200 g) and a_z (from -200 g to 200 g).

Figures 9 and 10 show the inverse of Figures 7 and 8. When the accelerometer is accelerated in both the x - and z -directions by

unknown values, the temperature differences ΔT_{x1} and ΔT_{z1} are measured by the x - and z -sensors, respectively. Then, the x - and z -accelerations a_x and a_z can be calculated by interpolation using the data shown in Figures 9 and 10. Thus, by using the two output values of ΔT_{x1} and ΔT_{z1} , the input (unknown) accelerations a_x and a_z can be obtained even with cross-axis sensitivity and nonlinearity.

Figure 9: x -acceleration a_x calculated from ΔT_{x1} and ΔT_{z1} .

Figure 10: z -acceleration a_z calculated from ΔT_{x1} and ΔT_{z1} .

Next, we focus on the problem discussed in Section 1 and by Nguyen et al. [10]. The acceleration considered exclusively for this problem is a_z . However, the range is very large, insofar as $a_z = -10,000$ g to $10,000$ g, as treated by Nguyen et al. [10]. The combined accelerations of the three components— a_x and a_z , or a_x , a_y , and a_z —are not considered, because doing so requires a considerable number of computer simulations. Moreover, it suffices only to change the z -acceleration for the purpose of studying this problem.

Figure 11 shows the computational result for the temperature differences measured by the z -sensor, ΔT_{z1} (filled black circles), and the x -sensor, ΔT_{x1} (unfilled black circles), for a large z -acceleration range of $a_z = -10,000$ g to $10,000$ g, with $a_x = a_y = 0$ g. The measured temperature difference, which is given by $\Delta T_{z1} = -10$ K as an example, can be produced by two accelerations: -1372 g and 359.5 g. Therefore, it is impossible to determine which acceleration is correct when $\Delta T_{z1} = -10$ K is measured with this accelerometer. As pointed out by Nguyen et

al. [10], when the acceleration is very large, “the sensor response is highly non-linear” so “the same response can be observed for two accelerations with different magnitudes and opposite signs.” Consequently, they considered only a smaller measurement range up to $\pm 5g$, for which good linearity was observed. However, this problem can be solved as explained below.

Figure 11: Temperature differences measured by the x -sensor ΔT_{x1} and z -sensor ΔT_{z1} for a large z -acceleration range ($a_z = -10,000$ g to $10,000$ g) with $a_x = a_y = 0$ g.

In Figure 11, the other temperature difference ΔT_{x1} produced by cross-axis sensitivity takes two different values of -17.620 K and -2.668 K for each a_z . If there were no cross-axis sensitivity, ΔT_{x1} would take a zero value when only the z -acceleration was added to the accelerometer. Therefore, by monitoring both ΔT_{x1} and ΔT_{z1} —in other words, by making use of cross-axis sensitivity—we can determine which acceleration value is correct even when the z -acceleration range is very large and the sensor response is highly nonlinear.

Note that another problem arises when graphing the relation between ΔT_{x1} and ΔT_{z1} , as shown in Figure 12. The curve intersects at $(\Delta T_{z1}, \Delta T_{x1}) = (-26.21 \text{ K}, -29.50 \text{ K})$, where the acceleration values are $a_z = -4864 \text{ g}$ and 5855 g . This makes it impossible to determine what acceleration produced these measured temperature differences. Fortunately, this problem can easily be solved by changing the position of the z -sensor, as explained below.

Figure 12: Relation between ΔT_{x1} and ΔT_{z1} .

For the above computational experiments, the height of the z -sensor was $0.1L$, where $L = 1 \text{ mm}$, as explained above. Figure 13 compares the results with three values for the height of the z -sensor: $-0.1 L$, $0.1 L$, and $0.3 L$. When the position of the z -sensor was lowered from $0.1 L$ to $-0.1 L$, the intersection point still existed and only shifted to the position $(\Delta T_{z1}, \Delta T_{x1}) = (-7.518 \text{ K}, -9.808 \text{ K})$ (thin line). On the other hand, by elevating the position of the z -sensor from $0.1 L$ to $0.3 L$, the intersection of the curve disappeared (dashed line). Thus, one combination of outputs ΔT_{z1} and ΔT_{x1} can determine a single acceleration value

of a_z , even when the z -acceleration range is very large (e.g., $-10,000$ g to $10,000$ g) and the sensor response is highly nonlinear.

Figure 13: Relation between ΔT_{x1} and ΔT_{z1} for three z -sensor positions.

Frequency Response

Courteaud et al. [3] stated that “the frequency response of the accelerometer is function of two phenomena. The first one corresponds to the frequency response of the fluid to the acceleration induced by the difference of temperature gradient on the sensitive axis. The second one corresponds to the frequency response of the detector to the temperature variation in the fluid.” In this section, we present a computational experiment performed to examine the frequency response of the fluid to the acceleration and show that the frequency response is a second-order system for horizontal acceleration and a third-order system for vertical acceleration.

Frequency Response for Horizontal Acceleration

We performed a computational experiment to study the frequency response of our accelerometer for the model size $L = 1$ mm. The acceleration with the frequency f in the horizontal direction (x -direction) added to the accelerometer is given by

$$a_x(t) = 10g \sin(2\pi ft) \quad (5)$$

The amplitude was kept at 10 g ($=98.1 \text{ m/s}^2$), and the frequency f was varied from 1 Hz to 5000 Hz. The power of the heater was 15 mW, the wall temperature was 300 K, and z -acceleration was the same as gravitational acceleration -1 g .

The magnitude M_x is defined by

$$M_x = 20 \log_{10} \left(\frac{\Delta T_\omega}{\Delta T_0} \right) \quad (6)$$

where ΔT_ω is the difference between the maximum and minimum temperatures produced at the temperature sensors by the sinusoidal acceleration given in (5), and ΔT_0 is the temperature difference measured at sensors T_{X1} and T_{X2} for a step response with the x -acceleration $a_x = 10 \text{ g}$. As the frequency decreased, ΔT_ω became closer to ΔT_0 until finally $M_x = 0$.

Figure 14 shows an example frequency response for x -acceleration with $f = 1 \text{ Hz}$ (thin line) measured by the two X -sensors T_{X1} and T_{X2} (the thick line and dot-and-dash line, respectively). The steady-state response with constant x -acceleration $a_x = 10 \text{ g}$ is also shown with a dashed line ($T_{X1} = 347.347 \text{ K}$) and long dashed line ($T_{X2} = 345.113 \text{ K}$). The maximum and minimum values of the frequency response with $f = 1 \text{ Hz}$ were almost the same as the steady-state values, which implies that $M_x = 0$. The delay of the phase of the frequency response was small. On the other hand, Figure 15 shows that, when the frequency was increased to 100 Hz, the maximum and minimum values of the frequency response became 346.925 K

and 345.655 K, respectively, and the delay of the phase shift was measured to be almost 60° .

Figure 14: Frequency response by x -acceleration with $\omega = 1$ Hz.

Figure 15: Frequency response by x -acceleration with $\omega = 100$ Hz.

In Figures 16 and 17, the dots indicate the computational results of the magnitude in decibels and the phase shift for the x -acceleration at various frequencies. Because the phase shift was from 0° to -180° , the x -acceleration was considered to have a second-order response ([12], pp. 10–34). Therefore, the transfer function can be written as

$$G(s) = \frac{1}{\left(\frac{s}{\omega_{n1}} + 1\right)\left(\frac{s}{\omega_{n2}} + 1\right)} \quad (7)$$

where ω_{n1} and ω_{n2} are the corner frequencies (approximately 62.3 and 1370 Hz). The damper factor is 2.45. The solid lines in

Figures 16 and 17 indicate the magnitude M_X in decibels, and the phase θ_X is given by

$$M_X = 20 \log_{10} |G(j\omega)| \quad (8)$$

$$\theta_X = \angle G(j\omega) \quad (9)$$

The curves of the theoretical Equations (7)–(9) agreed well with the computational results. Thus, the frequency response for the horizontal acceleration was proved to be a second-order system.

Figure 16: Magnitude M_X (dB) for x -acceleration.

Figure 17: Phase shift for x -acceleration.

Frequency Response for Vertical Acceleration

The acceleration with the frequency ω in the vertical direction (z -direction) added to the accelerometer is given by

$$a_z(t) = -g + 10g \sin(2\pi ft) \quad (10)$$

As before, the amplitude was kept at 10 g ($=98.1 \text{ m/s}^2$), and the frequency f was changed from 10 Hz to 2000 Hz. Because the computational results of the phase shift were from 0° to -270° , the response was considered to be a third-order ([12], pp. 10–34). Therefore, the transfer function can be written as

$$G(s) = G_1(s)G_2(s) \quad (11)$$

$$\begin{cases} G_1(s) = \frac{1}{\frac{s}{\omega_{n1}} + 1} \\ G_2(s) = \frac{1}{\left(\frac{s}{\omega_{n2}} + 1\right)\left(\frac{s}{\omega_{n3}} + 1\right)} \end{cases}$$

where ω_{n1} , ω_{n2} , and ω_{n3} are the corner frequencies of approximately 59.4, 325, and 731 Hz, respectively. The damper factor is 1.09. The solid lines in Figures 18 and 19 indicate the magnitude M_z in decibels, and the phase θ_z is given as follows:

$$M_z = 20 \log_{10} |G_1(j\omega)| + 20 \log_{10} |G_2(j\omega)| \quad (12)$$

$$\theta_z = \angle G_1(j\omega) + \angle G_2(j\omega) \quad (13)$$

The curves of the theoretical Equations (11)–(13) agreed well with the computational results. Thus, the frequency response for vertical acceleration was proved to be a third-order system.

Figure 18: Magnitude M_x (dB) for z -acceleration.

Figure 19: Phase shift for the z -acceleration.

Discussion and Conclusions

Section 2 introduced the principle to obtain a unique solution under the condition of a highly nonlinear sensor response with cross-axis sensitivity. Cross-axis sensitivity is not to be removed but rather exploited. For a thermal accelerometer, considering the temperature sensors for acceleration in only designated directions may be ineffective. By making data maps as shown in Figures 9 and 10, two (or three) responses from two (or three) temperature sensors can determine a unique set of two (or three) components of acceleration. Indeed, this can be done even when the acceleration range is very large, when the sensor response is highly nonlinear, and when cross-axis sensitivity is observed. As such, thermal accelerometers can be used under more severe conditions.

In this study, we did not try to improve the sensitivity of our thermal accelerometer or examine the effect of nonlinearity on sensitivity. In addition, we did not study the step responses due

to combined accelerations of the three components (viz., a_x , a_y , and a_z for short ranges; and a_x and a_z , or a_x , a_y , and a_z for very large ranges). As shown in Figures 12 and 13, the ambiguity (intersection of the curve) was easily removed by changing the height of the z -sensor when only z -acceleration was added to the accelerometer. However, when adding both x - and z -acceleration to the accelerometer, it was found that the points of intersection increased. This can be overcome by changing the positions of the temperature sensors and/or increasing the number of temperature sensors. Because such research requires many computer simulations and analyses, however, this will be discussed in future research.

As noted at the beginning of Section 3, the frequency response of the accelerometer is a function of two phenomena [3]. However, only the first phenomenon was treated here: namely, the frequency response of the fluid to acceleration induced by a difference in the temperature gradient. Future work will involve studying the second phenomenon: namely, the frequency response of the detector to temperature variation in the fluid.

The main conclusions are summarized as follows:

1. By monitoring the temperatures at two positions and making use of cross-axis sensitivity, a unique acceleration can be determined even when the range of vertical acceleration is very large, such as $-10,000$ – $10,000$ g.
2. Two (or three) responses from two (or three) temperature sensors can determine a unique set of two (or three) components of acceleration even when the acceleration range is very large, the sensor response is highly nonlinear, and cross-axis sensitivity is observed.
3. The frequency response for horizontal acceleration is a second-order system.
4. The frequency response for vertical acceleration is a third-order system.

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